

Übungsserie - Integralrechnung 2

1. Berechne (* freiwillig)

a) $\int \frac{2x+1}{x^2+x+3} dx =$

b) $\int \frac{x+1}{x^2+2x} dx =$

c) $\int \frac{x^2+2x-3}{x-2} dx =$

d) $\int \frac{x+1}{x^2+1} dx =$

e) $\int \frac{dx}{4x^2+9} =$

f) $\int \frac{dx}{x^2-2x+2} =$

g) $\int \frac{3 dx}{4x^2+4x+10} =$

h)* $\int \frac{dx}{(x-1)(x+3)} = (\text{Ansatz: } \frac{A}{x-1} + \frac{B}{x+3})$

2. Lösungen in zufälliger Reihenfolge ☺

I) $\arctan(x-1) + k$

II) $\ln |x^2+x+3| + k$

III) $\frac{1}{2} \ln |x^2+1| + \arctan x + k$

IV) $\frac{1}{2} \ln |x^2+2x| + k$

V) $\frac{1}{2} \arctan(\frac{2}{3}x + \frac{1}{3})$

VI) $\frac{x^2}{2} + 4x + 3 \ln |x-2| + k$

VII) $\frac{1}{6} \arctan \frac{2x}{3} + k$

h) $\frac{1}{4} \ln | \frac{x-1}{x+3} |$

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